## Time-Temperature-Transformation (TTT) Cure Diagrams: Relationships Between $T_g$ , Cure Temperature, and Time for DGEBA/DETA Systems

#### C. GUIBE and J. FRANCILLETTE\*

DGA/CREA, Département Polymères et Composites, 16 bis, avenue Prieur de la Côte d'Or, 94114 Arcueil, France

#### **SYNOPSIS**

Isothermal curing of a bisphenol A diglycidyl ether-based epoxy-resin-based, using an aliphatic polyamine, has been performed at temperatures between 20 and 60°C. Samples were cured isothermally at various intervals of time, and analyzed by differential scanning calorimetry (DSC). The glass transition temperature  $(T_g)$  and the conversion ratio cure determined by residual enthalpy analysis is used as an isothermal cure-controlled reaction. A time-temperature-transformation (TTT) isothermal cure diagram was carried out to include the time to vitrification and iso- $T_g$  curves. © 1996 John Wiley & Sons, Inc.

## INTRODUCTION

The conversion of linear epoxy resins into threedimensional cross-linked or thermosetting materials is performed by curing reaction. Curing kinetics of epoxy resins has been studied with different techniques. In the present work, isothermal cure was studied by differential scanning calorimetry (DSC).<sup>1,2</sup>

The isothermal curing reaction of an epoxy resin is complicated as a consequence of the interaction between curing chemical kinetics and other physical processes, such as gelation and vitrification, which causes important changes in the reacting system macroscopic physical properties.<sup>1,3</sup>

A convenient summary of the changes occuring during cure of a thermosetting system is the isothermal time-temperature-transformation (TTT) cure diagram described by Gillham et al.<sup>3,4</sup> and schematically shown in Figure 1. It displays the changes of the material states and characterizes the changes in the material during isothermal cure as a function of time. Material states include liquid, sol-glass, sol/gel-rubber, gel-rubber, sol/gelglass, gel-glass, and char. The various changes occurring in the material during isothermal cure are characterized by contours of the time to reach the events.

This paper studies the temperature and time conditions of an epoxy resin isothermal cure. The glass transition temperature  $(T_g)$  is used as a parameter to monitor the curing reaction.  $T_g$  does not increase linearly with conversion. The unreacted material  $T_g = T_{g_0}$  and the fully reacted material  $T_g$  $= T_{g_{\infty}}$ . Vitrification occurs when the glass transition temperature  $T_g$  becomes equal to the curing temperature  $T_c$ .

The aim of this work is to study the feasibility of using  $T_g$  as a measure of the chemical conversion. The time-temperature superposition of  $T_g$  versus ln time DSC data provides a kinetically controlled master curve, as well as the apparent activation energy of polymerization. The master curve and the reaction activation energy are used in the calculating iso- $T_g$  contours prior to vitrification and also the vitrification contour. The basis of the approach is the fact that there is a one-to-one relationship between  $T_g$  and conversion which is independent of cure temperature, and the kinetically controlled reaction is over vitrification.

<sup>\*</sup> To whom correspondence should be addressed.

Journal of Applied Polymer Science, Vol. 62, 1941-1951 (1996)

<sup>© 1996</sup> John Wiley & Sons, Inc. CCC 0021-8995/96/111941-11



Figure 1 Time-temperature-transformation isothermal cure diagram for a thermosetting system. Source: Gillham.<sup>3</sup>

## EXPERIMENTAL PART

## **Starting Materials Reactants**

The difunctionnal epoxy monomer used for this work was a diglycidylether of BisphenolA (DGEBA) (DER 332, DOW Chemical Co.) cured with a pentafunctionnal aliphatic amine. The chemical structures of the reactants are shown in Figure 2. The reaction was stoichiometric, with one epoxy group reacting with one amine hydrogen according to their respective equivalent weights: DER 332 = 170 g/Eq; DETA = 20.63 g/Eq. The mixture was prepared at room temperature; immediately after mixing, the viscous liquid was weighted accurately in open aluminium pans and cured in the DSC oven. The reactive mixture was poured into numerous aluminium weighing pans and stored in the freezer part of a refrigerator (-15°C) for no more than 8 h. The glass transition temperature of the uncured mixture  $T_{g_0}$ was -40°C.

### **DSC Measurements**

A Perkin-Elmer instrument (DSC 7) was used to measure the  $T_g$  and the residual exotherm ( $\Delta Hr$ ) of the reaction the material being firstly isothermally cured at prespecified times.

The samples were kept cold before the experiments. Handling was carried out at room temperature just before curing. The isothermal curing was performed at five different temperatures  $(20, 30, 40, 50, \text{ and } 60^{\circ}\text{C})$ .

The instrument operated with a nitrogen flow rate of about 30 cm<sup>3</sup> min<sup>-1</sup> through the cell. An empty pan was used as the reference material. For isothermal measurements, samples were inserted at  $-15^{\circ}$ C, then heated at  $T_c$  with a programmed rate of 100°C min<sup>-1</sup>.

After curing, each specimen was quenched from  $T_{\rm cure}$  to -40 or -60°C at a programmed rate of 200°C min<sup>-1</sup> and then submitted to a temperature scan from -40 or -60°C to 250°C at 10°C min<sup>-1</sup> to determine the  $T_g$  of the material after cure and  $\Delta Hr$  of the remaining reaction.

The highest  $T_g$  value observed for extended cure times in this data set is 86°C, obtained at 60°C.

Loss of weight during temperature scans (30–850°C) on the uncured resin-hardener mixture was measured in flowing nitrogen using a thermogravimetric analyzer equipped with a controller (Perkin-Elmer TGS2, system 4 microprocessor). The rate of temperature change was  $10^{\circ}$ C min<sup>-1</sup>. Figure 3 shows that the onset temperature was located at 320°C. The material's relatively good temperature stability should not hide the fact that we worked with a low temperature system because of the presence of a very reactive aliphatic hardener. Furthermore, at 250°C, the loss of weight was approximately 4%, which might have a negative effect for high temperature composite applications.

## **RESULTS AND DISCUSSIONS**

 $T_g$  was measured as the halfway point of  $\Delta Cp$ , when the polymer undergoes a transition from the



#### DETA

Figure 2 Chemical structures of the reactants.



Figure 3  $T_g$  temperature scan for uncured DER 332/DETA.

glassy state to the rubbery state. The apparent conversion ratio of the curing reaction is calculated from the residual enthalpy  $\Delta Hr$  of the partially cured resin and from the total enthalpy of reaction ( $\Delta H_T = -581.5 \text{ J g}^{-1}$ ) corresponding to one ideal unreacted mixed sample without curing treatment:

$$\alpha = \left[ \Delta H_T - \Delta Hr \right] / \Delta H_T$$

## Experimental T<sub>g</sub> Versus Residual Heat of Reaction

 $T_g$  evolution and the corresponding residual heat of reaction  $\Delta Hr$  of the material cured at 40°C for different times are shown in Figure 4. Both  $T_g$  and  $\Delta Hr$ 



Figure 4 DSC temperature scans of samples isothermally cured at 40°C for different times.



Figure 5 Residual exotherm versus  $T_g$  for DER 332/DETA (1:1).

change regularly with cure time;  $T_g$  increases while  $\Delta Hr$  decreases until the reactants are fully consumed (because of the crosslinking increase density in the network).

Figure 5 shows the residual exotherm versus  $T_g$  plotted for different cure temperatures (20, 30, 40, 50, and 60°C). The data are fitted with a third-order polynomial shown by the solid line in this



**Figure 6**  $T_g$  versus fractional conversion (also illustrated is  $\alpha_v$ , the conversion ratio at vitrification).



**Figure 7** Conversion ratio versus time at  $T_c = 50^{\circ}$ C.

figure. For this epoxy-amine system, there is a unique one-to-one relationship, independent of cure temperature between either  $T_g$  and the residual exotherm or between  $T_g$  and conversion. The

same data are also plotted in Figure 6 as  $T_g$  versus fractional conversion. In the following analysis and discussions,  $T_g$  will be treated as a direct measure of the extent of reaction.



Figure 8  $T_g$  versus ln (time) at different cure temperatures.



**Figure 9** Dependence of limiting conversion ratio  $\alpha_{\infty}$  and conversion degree at vitrification  $\alpha_{\nu}$  on the cure temperature.

## Dependence of the Conversion Ratio with the Curing Conditions

For a given curing temperature, the conversion ratio increases with a sigmoidal shape and tends to have a limiting conversion ratio, which depends on this cure temperature (Fig. 7).

When  $T_c < T_{g_{\infty}}$ , isothermal curing undergoes two different stages. The first one is controlled by the chemical reactivity of functional groups; the curing reaction takes place in the liquid state, and the  $T_{e}$  of the system is lower than the  $T_c$ . The reaction rate depends on  $T_c$  until  $T_g = T_c$ . At this point, the second stage of curing starts. The system vitrifies, and the reaction decreases considerably until the reaction becomes practically inhibited by a restricted reacting groups mobility, which prevents full conversion. The reaction time required for reaching  $T_g = T_c$  is called vitrification time  $t_v$ . Its values at different  $T_c$  obtained from  $T_g$  data versus time are shown in Figure 8. Isothermal vitrification  $(T_g = T_c)$  at each cure temperature is designated by an arrow. When the system reaches the glassy state, the chemical reaction becomes controlled by diffusion,<sup>3,5</sup> and the conversion ratio tends to a practically constant limiting value  $\alpha_{\infty}$ . Figure 9 shows the two stages in a diagram of conversion ratio versus curing temperature. The conversion at vitrification (when  $T_g = T_c$ ) was

graphically obtained using the relationship between  $T_g$  and conversion. The conversion ratio at vitrification time  $\alpha_v$  determines the progress of curing controlled by chemical processes. The difference between  $\alpha_{\infty}$  and  $\alpha_v$  shows the progress of the cross-linking reaction in the glassy state controlled by diffusion.

The data for the extrapolated time to vitrification versus the temperature of isothermal cure were plotted using a Arrhenius law: logarithmic time versus 1/T (K). The activation energy of vitrification for isothermal transformation is ( $\Delta E = 11.24$ kcal mol<sup>-1</sup>).

## Dependence of the Glass Transition Temperature on the Curing Conditions

During the isothermal curing at  $T_c$ , the  $T_g$  of the system increases with the curing time  $t_c$  due to the increase in the network crosslinking density. For samples cured at  $T_c < T_{g_{\infty}}$ , deceleration has been noticed to occur near  $T_g = T_c$  because of system vitrification. Beyond the vitrification time,  $T_g$  becomes higher than the curing temperature; as a result, the system is annealed at a lower temperature than  $T_g$ , thus, a structural relaxation process or physical aging in the amorphous phase. On the DSC scanning up from -40 or -60°C through  $T_g$ , these



**Figure 10** A typical DSC scan of samples isothermally cured at 20°C for different times, showing  $T_e$  and the endothermic annealing peak.

samples showed an endothermic peak superposed to  $T_g$ . Figure 10 illustrates the operational definition of  $T_g$ . Then  $T_g$  increases slowly with the annealing time at a temperature  $T_c < T_g$  and approaches asymptotically to a limiting value depending on  $T_c$ .

Therefore, to be able to obtain curing in the glassy state, values of  $T_g$  cure must be greater than  $T_c$  + 26°C (Fig. 11).

#### **Time-Temperature Superposition of DSC Data**

Time-temperature shifts of  $T_g$  versus log time at different cure temperatures yields to a master curve for the reaction at an arbitrary reference temperature.<sup>5</sup>

For the time-temperature superposition, the rate expression of epoxide conversion is not needed.<sup>5,6</sup> In a first approach, the data can be treated as if the reaction was only kinetically controlled, neglecting the diffusion contribution. Therefore, the reaction rate can be described mechanistically by the usual kinetic rate equation:

$$d\alpha/dt = k_{(T)} \times f(\alpha) \tag{1}$$

where  $k_{(T)}$  is the reaction rate constant which depends on temperature only.  $k = A \exp(-Ea/RT)$ , with A, Ea, and R having their usual definition, and T is expressed in  $K. f(\alpha)$  is assumed to be a function

of conversion independent of temperature. Rearranging eq. (1), integrating at constant temperature, and taking the natural logarithm, we obtain

$$\ln \int_0^\alpha \frac{d\alpha}{f(\alpha)} = \ln k_{(T)} + \ln t$$
 (2)

The left-hand side of the equation is only a function of conversion ( $\alpha$ ) and, thus, also a function of  $T_g$  only

$$F(T_g) = \ln k_{(T)} + \ln t$$
 (3)

This equation describes the variation of  $T_g$  with cure time and temperature. This equation is valid for all cure temperature as long as the reaction mechanism remains kinetically controlled. Equation (2) suggests that for a kinetically controlled reaction, all isothermal  $T_g$  versus log (time) curves at different cure temperatures should be superimposed by simply shifting all curves horizontally (relative to a curve at a fixed reference temperature). A common master curve can be obtained. The resulting curve with  $T_{ref} = 50^{\circ}$ C is shown in Figure 11. Note that vitrification points at all cure temperatures on the master curve are marked by arrows.

A satisfactory superposition is obtained. The deviations from the master curve occur near the system vitrification and obviously at  $T_g > T_c$ , which cor-

responds to diffusion control due to low segmental mobility.

The shift factors  $A_{(T)}$  listed in Table I are defined as the ln time difference at constant  $T_g$  (i.e., constant conversion) between the  $T_g$  versus log time curve for temperature  $T_c$  and the curve for an arbitrary reference temperature  $T_{ref}$ 

$$A_{(T)} = \ln t_{(ref)} - \ln t(T_c)$$
  
=  $(-Ea/R)(1/T_c - 1/T_{ref})$  (4)

#### **Activation Energy**

The apparent activation energy of the reactions is determined from eq. (4). Plotting the master curve shift factor against reciprocal cure temperature (1/K) gives a straight line with a slope -E/R, as shown in Figure 12. The apparent activation energy thus obtained is 16.05 kcal mol<sup>-1</sup> (67.08 kJ mol<sup>-1</sup>).

# Construction of Iso- $T_g$ Contours and Vitrification Curve in the Isothermal TTT Diagram

## Iso-T<sub>g</sub> Contours

The reaction activation energy determined in the previous section can be used for constructing an iso-

Table I	Shift	Factor	Relative	to	50°C	for
Different	Cure	Tempe	eratures			

Cure Temperatures (°C)	Shift Factors $[A(T)] = [\ln(t_{50}) - \ln(t_T)]$		
20	-2.554		
30	-1.481		
40	-0.644		
50	0		
60	0.840		

 $T_g$  contour if, in addition, a data point of the contour is known.

The relationship between times to reach a fixed  $T_g$  at different cure temperature for a kinetically controlled reaction is given by eq. (4), rearranged as follows:

$$-Ea/RT_{1} + \ln(tT_{g_{1}})$$
  
=  $-Ea/RT_{2} + \ln(tT_{g_{2}})$  (5)

where  $t(T_{g_1})$  is the time needed to reach a given  $T_g$ at cure temperature  $T_1$ , and  $tT_{g_2}$  is the time needed to reach the same  $T_g$  at cure temperature  $T_2$ . Thus, if a time to reach a particular  $T_g$  at one cure temperature (i.e.,  $tT_{g_1}$  at  $T_1$ ) is known, then the time to



Figure 11 Time-temperature superposition:  $T_{g}$  versus ln (shifted) time different cure temperatures for a reference temperature at  $T = 50^{\circ}$ C.



**Figure 12** Arrhenius plot shift factor  $A_{(T)}$  versus reciprocal cure temperature (1/K).

reach the same  $T_g$  at different temperature (i.e.,  $tT_{g_2}$  at  $T_2$ ) can be calculated from eq. (5).

Each point on the master curve provides a necessary data point (i.e., a time  $tT_{g_1}$ ) to reach a particular  $T_g^*$  at  $T_1 = 50$ °C, which can be used in eq. (5), together with the activation energy for the reaction determined in the previous section, for the calculation of an iso- $T_g = T_g^*$ .

The calculated results are incorporated into the TTT diagram in the form of a series of iso- $T_g$  contours by plotting the cure temperature  $T_c$  against the logarithm of the times to reach a particular  $T_g^*$ . Figure 13 shows the calculated iso- $T_g$  (for  $T_g = -35$  to  $+75^{\circ}$ C).

#### Vitrification Curve

Vitrification reaction occurs when the glass transition increases up to the temperature of cure and indicates the transition from a rubber to a gelled glass (if gelation has occurred) or from a liquid to an ungelled glass (if gelation has not occurred).

Since the master curve covers the entire range of  $T_g$ , the virtrification curve can be calculated. The iso- $T_g$  relation [eq. (5)] is valid until the material vitrifies and can be used to estimate the isothermal times of vitrification. Each point on the master curve (Fig. 11) provides a necessary data point [i.e., a time  $(tT_{g_1})$  to reach a particular  $T_g$  at  $T_c = 50^{\circ}$ C], which can be used for calculation, and  $t_{vit}$  is given by:

$$\ln t_{vit} = -Ea/R[1/T_{cure} - 1/T_g] + \ln t_{cure}$$

Figure 13 shows the vitrification curve and different iso- $T_g$  contours (for  $T_g = -35 + 75$ °C) in the form of an isothermal TTT diagram. The vitrification curve is S-shaped.

The times to vitrification undergoes a minimum at a cure temperature just below  $T_{g_{\infty}}$  because of the competing effects of both the reaction rate constant and the extent of conversion at vitrification increasing with temperature.

The data for an isothermal TTT diagram can be represented in a line versus 1/T(K) plot, from which the apparent activation energy for the transformation can be determined. The line time versus 1/T(K) plot is presented in Figure 14. The apparent energy for vitrification is given by the slope. The value of the vitrification energy is 12.34 kcal mol<sup>-1</sup>.

## CONCLUSION

The analysis of the relations between the cure time and temperature has led to the following conclusions.

1)  $T_g$  is an appropriate parameter for monitoring the cure process. The results show that



Figure 13 Calculated isothermal TTT diagram showing iso- $T_g$  contours and vitrification curve.

 $T_g$  for an epoxy-aliphatic amine system is a function of conversion independent of the cure temperature. A one-to-one relationship between  $T_g$  and conversion is found for the DGEBA/DETA system.

 $T_g$  versus ln (t) at different cure temperatures, we obtain a master curve at a reference cure temperature (50°C), according to the assumption that the reaction is purely kinetically controlled. From this curve, we found an activation energy is closed to 16.05

2) By plotting time-temperature shifts of the



Figure 14 Ln time versus 1000/T(K) and apparent activation energy for vitrification.

kcal  $mol^{-1}$ . The isothermal vitrification points at all cure temperatures lie on the master curve, which indicates that the reaction before vitrification is only kinetically controlled. Perturbations of the data from the master curve occur after vitrification, revealing the onset of diffusion control.

- 3) In the TTT cure diagram, the master curve, together with the calculated activation energy, are used as a basis for a simple calculation of vitrification curves, and iso- $T_g$  contours are presented.
- 4) The reaction vitrification energy determined from isothermal TTT diagram is calculated  $(E_v = 12.34 \text{ kcal mol}^{-1}).$

The authors would like to thank the Direction de la Recherche et de la Technologie for Financial support.

## REFERENCES

- R. B. Prime, In *Thermal Characterization of Polymeric* Materials, Vol. 5, E. A. Turi, Ed., Academic Press, New York, 1981, pp. 435-569.
- J. M. Barton, in Epoxy Resins and Composites; Advances in Polymer Science 72, I. K. Dusek, Springer-Verlag, Berlin, 1985, pp. 112–154.
- 3. J. K. Gillham, Polym. Eng. Sci., 26, 1429 (1986).
- J. B. Enns and J. K. Gillham, J. Appl. Polym. Sci., 28, 2567 (1983).
- G. Wisanrakki and J. K. Gillham, J. Coat. Techol., 62, 35-50, 783 (1990).
- S. Gan, J. K. Gillham, and R. Prime, J. Appl. Polym. Sci., 37, 803-816 (1989).

Received January 9, 1996 Accepted June 12, 1996